Supervised Intentional Process Models Discovery using Hidden Markov Models

Ghazaleh Khodabandelou, Charlotte Hug, Rebecca Deneckere, Camille Salinesi

To cite this version:

HAL Id: hal-00803875
https://hal-paris1.archives-ouvertes.fr/hal-00803875
Submitted on 10 Apr 2013

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Supervised Intentional Process Models Discovery using Hidden Markov Models

Ghazaleh Khodabandelou, Charlotte Hug, Rébecca Deneckère, Camille Salinesi
Centre de Recherche en Informatique
University of Paris 1 Panthéon-Sorbonne
Paris, France

Abstract—Since several decades, discovering process models is a subject of interest in the Information System (IS) community. Approaches have been proposed to recover process models, based on the recorded sequential tasks (traces) done by IS’s actors. However, these approaches only focused on activities and the process models identified are, in consequence, activity-oriented. Intentional process models focus on the intentions underlying activities rather than activities, in order to offer a better guidance through the processes. Unfortunately, the existing process-mining approaches do not take into account the hidden aspect of the intentions behind the recorded user activities. We think that we can discover the intentional process models underlying user activities by using Intention mining techniques. The aim of this paper is to propose the use of probabilistic models to evaluate the most likely intentions behind traces of activities, namely Hidden Markov Models (HMMs). We focus on this paper on a supervised approach that allows discovering the intentions behind the user activities traces and to compare them to the prescribed intentional process model.

Keywords—intention mining; process modeling; supervised learning; process discovery

I. INTRODUCTION

While many process models have been proposed to guide information systems engineering, still much remains to be done to understand their actual implementation. Analyzing the traces enacted by Information System Engineering (ISE) stakeholders allows detecting the gap between the prescribed process model and what is actually done by the stakeholders. Such gap occurs when the prescribed process model is under-matching (mediocre precision with the presence of noisy behaviors), over-matching (mediocre generalization which recovers only current behaviors) or ill-matching (missing or/and irrelevant behaviors). Any of these gaps could cause the failure of the project or at least be a catalyst to lower the quality of software products.

Several process mining approaches have been proposed to discover process models from event logs [6,7,10,17]. While these methods help to recover the sequences of activities and to extract information from those sequences, they overlook the hidden intentions that generate them. Intentions are important as they capture what the stakeholders intend to perform [1]. To fulfill their intentions, actors perform a set of activities; they also may change their intentions during the process enactment and sometimes have random behaviors. As a result, we believe that whereas sequences of activities represent a set of actors’ behaviors executed one after another, the fundamental process behind them is mostly intentional. However, discovering intentional process model from event logs is part of a whole new field of researches, which we call Intention Mining.

The main objective of Intention Mining is to extract sequences of actors’ activities from an event log to evaluate and predict the actors’ intentions related to those activities [36][37],[38]. Knowing the intentions underlying actors’ activities allows improving the actors’ guidance through their tasks. As a matter of fact, if we know why an actor is performing some activities, we can have a better handling of what he may want to do on his next step and offer him better recommendations. Intention mining can be useful at different levels, for instance: at the design level, to identify the underlying intentions hidden in the logs in order to define the followed process model; at the analysis level, to identify the gap between a prescribed process model and the activities actors are actually performing; at the application level, to recommend steps to the actor at run-time, following logs history.

This work focuses on the discovery of the intentions hidden in the logs and on the intentional process model enactment. To rebuild the process model (the followed model that generates the activities’ traces) and evaluate the intentions, we use Hidden Markov Models (HMMs) [8] and Map, an intentional process metamodel [1]. Map allows representing flexible process models, enacted in a dynamic way since the sections of a Map process model can be executed non-sequentially and as long as intentions are not completely fulfilled. We propose a two-step method. The first step consists in a training phase to estimate the parameters of HMM using sequences of activities whose intentions are known. The second step consists in recovering the intentions in a fully automated way by using the estimated parameters on a new dataset. In this paper, we describe a case study that consists in analyzing the traces produced by students designing entity-relationship diagrams.

This paper is organized as follow: in section 2, we present the related works. In section 3, we describe the technical contribution based on HMMs. In section 4, we present the results of the case study and we conclude this paper in section 5.
II. RELATED WORK

HMMs are applied in many fields where the objective is to rebuild the hidden states of observed processes, such as speech recognition [25] and bioinformatics [30].

A comparable kind of challenge arises in process mining, where the goal is to extract observed activities from event logs to recover the original workflow that produced the logs. These event logs contain the traces of process executions. In process mining approaches, the objective is generally to discover the sequence of tasks and activities underlying processes. To do so, these approaches extract the information from event logs using different algorithms and techniques such as classification and learning techniques [2].

One approach to discover the processes is Machine Learning (ML) [14, 18]. Depending on the type of inputs, there are various ML approaches: supervised, unsupervised, semi-supervised and reinforcement. Supervised-learning is based on two steps: (a) in a training step, a learning algorithm is applied on observations (independent variables) to train a classifier, (b) in a prediction step, the trained classifier can be tested using a testing set of observations, and most importantly, the classifier can be applied on any new dataset. Figure 1 illustrates this approach.

In [14], a workflow is modeled with HMMs that reflect the process model on another level. This work does not address the intentional dimension of processes. As a result, it is for instance not possible to reason about the importance of intentions or to recognize whether an instance of workflow deviates from the goals of the project.

In this paper, we apply supervised HMMs in the line of several former works.

In [2], HMMs are considered as versatile and relevant for process mining but HMMs unsupervised approaches are complicated: (a) there are computational challenges due to time-consuming iterative procedures, (b) the number of states (as algorithm inputs) should be known, (c) the result of HMMs is not very understandable for the end-user.

In [16, 27], three different inference algorithms illustrate process discovery – they infer process models from event logs: RNet, Ktail and Markov.

(a) RNet [31] is a statistical approach that characterizes a state depending on the past behaviors. RNet generates a Deterministic Finite State Machine (DFSM), i.e., each state has only one transition for each possible input. It is robust to noise but is very time-consuming in the training phase, the size of the net increases with the number of token’s types and it requires to evaluate many parameters.

(b) Ktail [26] is an algorithmic approach that evaluates the current state depending on future behavior. The input is a set of sample strings and the output is a Finite State Machine. One can control the complexity of the algorithm when the number of states increases by DFSM. The disadvantage of this method is that it is not very robust to noise.

(c) Markov is a hybrid, between the statistical and algorithmic approaches looking at the neighboring past and future behavior to define the future state. It is robust to noise with a complexity that is controllable and has a deterministic FSM. However, this algorithm tries to discover only the processes from event logs and does not consider the actors’ intentions behind these processes.

Another work, [12], uses HMMs as a conformance checking technique by measuring similarities between Markov models using a distance metric. It enables the authors to evaluate the quality of mined processes. The workflows modeled in Petri nets are mapped to HMMs but the hidden states of processes are not taken into account.

Fig. 1. Illustration of supervised learning.
Nevertheless, all these works consider the hidden states of HMMs as the instances of the process while we consider the hidden states as the intentions that generate the observed sequences of activities. We do not model a process only as a set of tasks as Petri nets do, but as the intentions behind the activities’ sequences. Moreover, many classical techniques of classification like SVM (Support Vector Machine) [28] cannot deal with the noise (incomplete or irrelevant data) and do not support the variability of data sequences - they only accept a prescribed length of sequences whereas sequences of activities’ lengths are variable depending on the actors’ purposes.

III. TECHNICAL CONTRIBUTION

Our technical proposition consists in:

- Modeling an intentional process model using HMM. The HMM fits the intentional process model since it models hidden states, i.e., intentions, found in observable data, i.e., traces of activities.
- Estimating the parameters of the HMM based on traces obtained from practical uses of the intentional process model.
- Predicting the next intentions and consequently the next activities using the estimated parameters of HMM.
- Evaluating the intentions associated to a sequence of activities using the Viterbi Algorithm (VA), given the parameters of the HMM. We discuss the performances of this evaluation in section IV.

Our work relies on the assumption that the realization of traces of activities follows a stochastic process. A stochastic process represents an evolution, discrete or continuous, of a random variable. Thus, we need to choose a statistic model that allows (a) knowing the observed sequences; if they are significant or only accident outcomes, (b) analyzing the observed sequences over time, (c) modeling the latent states of these observed sequences, (d) extracting the characteristics of observed and latent sequences. Among the probabilistic models we select HMMs [21,25] for several reasons. As described in the previous section, the other methods do not fit the intentional model. HMMs are applied widely in bioinformatics’ field [20, [30]. Nevertheless, as indicated earlier, several applications of HMMs in process mining [12, 14] consider the hidden states as the process instance. The contribution of this paper consists in applying HMM to discover intentions from traces of activities, that we name Intention Mining [38].

HMMs are a special kind of stochastic process that captures the relations between an observable sequence (the activities) and their hidden states (associated intentions). More precisely, the framework of HMMs allows focusing on several problems such as (a) How to estimate the parameters of the HMMs? (b) What is the probability of a given activities sequence? (c) What are the most probable intentions associated to a given activities sequence? The last question is of great interest for our work since we aim at finding the hidden intentions associated to a sequence of traces of activities. We present in the following subsections an overview of HMMs.

A. Hidden Markov Models (HMMs)

1) Definition

A HMM is a statistical signal modeling formalism that allows modeling a sequence by a finite number of states that alternate. HMMs are very flexible due to latent data that allows modeling the structure of complex temporal dependencies. The systems modeled by HMMs are based on two complementary Markov processes, i.e., specific types of stochastic processes.

To understand what is a Markov process, let \((X_1, ..., X_T)\) be a sequence of random variables with length \(T\) generated by a Markov chain of order \(m\) (or with memory \(m\)), where \(m\) is finite. The generating process is:

\[
\Pr(X_t = x_t | X_{t-1} = x_{t-1}, X_{t-2} = x_{t-2}, ..., X_1 = x_1) = \Pr(X_t = x_t | X_{t-1} = x_{t-1}, X_{t-2} = x_{t-2}, ..., X_{t-m} = x_{t-m})
\]

\[f o r \ t > m. \tag{1}\]

This means that for a Markov chain of order \(m\), the transition to the next state depends only on the \(m\) previous states. The choice of \(m\) indicates how far in the past one has to look to know the probability of the next state.

In the context of HMMs, we need to define two Markov processes. A first Markov process models the hidden state of the system. A second Markov process models the observations of the system, knowing that this second process depends on the hidden states. In our framework, the hidden states are the intentions and the observations of the system are the traces of activities. The topological structure of HMMs allows defining, according to the context, dependences between hidden states and/or observed data from the past to the future ones.

2) Models of HMMs

Choosing the right order for Markov chains in an HMM is a challenge since the orders of the chains define the behavior of the HMM. As a first step, we will work with a MIMO model.

A MIMO model means that among the different orders of Markov chains, we rely on a Markov chain of order 1 and a Markov chain of order 0. A Markov chain of order 1 is a process where the transition to the next state depends only on the current state (also called Markov property). A Markov chain of order 0 is a process where the transition to the next state does not depend on any state. We now define the order for each Markov chain.

Definition 1: Hidden process. For a given time \(t\), the state of the system \(I_t\) is only dependent on the state of the system at the previous time step \(I_{t-1}\). This definition applies to the intentions (model \(M_I\)). A sequence of intentions is denoted by \(I_{1:T} = (I_1, ..., I_T) \in S^T\), with \(S\) being the set of intentions and \(T\) being the length of the sequence. A homogeneous Markov chain, which parameter is denoted by \(q\), models the hidden process of intentions with:

\[
q(u,v) = \Pr(I_{t+1} = v | I_t = u), \forall u,v \in S, \tag{2}
\]

and
\[ q(u) = \mathbb{P}(I_1 = u), \forall u \in S. \quad (3) \]

The parameter \( q \) in (3) contains the probabilities of intention at the initial state and in (2) the transition probabilities for the following intentions.

**Definition 2: Observed process.** For a given time \( t \), the observation \( A_t \) does not depend on any previously observed sequence. This definition relates to the sequence of activities (model M0). We denote an observed sequence of activities' activities by \( A_{1:T} = (A_1, \ldots, A_T) \in \mathbb{R}^T \), with \( R \) being the set of activities. The emission probability \( p \) of an observation \( a \in R \) for a given intention \( u \in S \), is given by:

\[ p_u(a) = \mathbb{P}(A = a | I = u). \quad (4) \]

\( P \) and \( q \) are the parameters of the HMM, namely the transition and emission probabilities. The transition probabilities are the probabilities of a hidden state at time \( t \) to reach another hidden state at time \( t + 1 \) (or to stay in the same state) as shown in figure 2.

\[ \cdots A_{t-1} \quad A_t \quad A_{t+1} \cdots \]

\[ \cdots I_{t-1} \quad I_t \quad I_{t+1} \cdots \]

**Fig. 2. Transitions of intentions and emissions of activities in a M1M0 HMM.**

The emission probabilities are the conditional probability distribution of the observed variables in a given hidden state at time \( t \). This model is a M1M0 model since the hidden process is a first-order Markov chain and the observed process is a zero-order Markov chain. In other words, this means that the choice for executing an activity among all while enacting a process model is not isolated, but correlated to other activities achieved before.

As an example, we consider a case with three hidden intentions \( \{I_1, I_2, I_3\} \) and four observed activities \( \{a_1, a_2, a_3, a_4\} \). The associated M1M0 model is described by the probability distribution of the initial intention and by two matrices: one \( 3 \times 3 \) matrix for the transition probabilities of hidden intentions denoted by \( I \) (6) and a \( 3 \times 4 \) matrix for the emission probabilities of observed activities for each intention, denoted by \( A \) (7).

\[
I = \begin{pmatrix}
q(I_1, I_1) & q(I_1, I_2) & q(I_1, I_3) \\
q(I_2, I_1) & q(I_2, I_2) & q(I_2, I_3) \\
q(I_3, I_1) & q(I_3, I_2) & q(I_3, I_3)
\end{pmatrix} \quad (6)
\]

\[
A = \begin{pmatrix}
p_1(a_1) & p_1(a_2) & p_1(a_3) & p_1(a_4) \\
p_2(a_1) & p_2(a_2) & p_2(a_3) & p_2(a_4) \\
p_3(a_1) & p_3(a_2) & p_3(a_3) & p_3(a_4)
\end{pmatrix} \quad (7)
\]

**B. Estimation of parameters**

Once we chose the model, we have to estimate the parameters of the HMM. There are two approaches to estimate the parameters of a HMM: supervised and unsupervised. The supervised approach is used when the segmentation of some activities' sequences into intentions is known while the unsupervised approach is used when the segmentation of any activities sequence is unknown.

We adopt the supervised approach in this paper. As indicated in section II, the supervised approach involves two phases. The first phase is a learning phase that consists in training the algorithm with sequences of activities to find the parameters of the HMM. For these sequences, the segmentation is known, i.e., the intentions related to the traces of activities are known. The second phase of the supervised approach, defined in subsection C, consists in the evaluation of the intentions related to a given activities' sequence.

The estimation of the parameters consists in finding the probability distribution of traces - the couple \( (p, q) \) defined in (2) and (4). If a sequence of activities \( A_{1:T} \) is available and the corresponding intentions are known, the computation of the estimates for \( (p, q) \) consists in using the Maximum-Likelihood Estimation (MLE) [11]. This method estimates the parameters \( q(u,v) \) and \( p_u(a) \) such that they analytically maximize the likelihood of having simultaneously the intentions \( I_{1:T} \) and the sequence of activities \( A_{1:T} \).

It amounts in counting the number of transitions from one intention to another and the number of apparitions of each activity during each intention as shown below:

\[ \hat{q}(u,v) = \frac{\text{Num}(u,v)}{\sum_{u \in S} \text{Num}(u,v)} \quad (8) \]

and

\[ \hat{p}_u(a) = \frac{\text{Num}(a|u)}{\text{Num}(a)} \quad (9) \]

where \( \text{Num}(u,v) \) in (8) denotes the number of transitions from intention \( u \) to intention \( v \), \( \text{Num}(a) \) in (9) denotes the number of apparitions of activity \( a \) and \( \text{Num}(a|u) \) denotes the number of apparitions of activity \( a \) while the intention is \( u \).

These parameters allow learning the distribution of the activities and intentions in the process model. This learning phase is necessary for the next step to evaluate the most likely intentions associated to a given activities' sequence.

**C. Evaluation of intentions’ sequences**

Once the parameters of the HMM are estimated, we want to be able to identify the most likely set of intentions associated to any sequence of activities. To do so, given a sequence of activity \( A_{1:T} \) of length \( T \), one could generate all the possible intentions of length \( T \). Then, for each intention \( I_{1:T} \), one could compute the probability \( \mathbb{P}(A_{1:T} | I_{1:T}) \). However, this is a brute-force search and it cannot be used to compare all the possible intentions for complexity reasons. For instance, if the number of intentions is \( C \), the complexity will be \( C^T \), which increases exponentially with \( T \).
Instead, the VA [23] is used to obtain, from a given observed sequence, the most likely hidden sequence of intentions that might generate it. The VA is commonly used in the context of HMM; this algorithm is able to calculate the probability that an observation or an intention has been changed into another, and radically simplifies the complexity of the search for the most likely hidden sequence. Thereby, the exponential complexity becomes linear.

This corresponds to the second phase of the supervised approach. As we mentioned earlier, to use the VA, it is necessary to know the estimated parameters obtained in the previous phase. We note that a given sequence of activities, with length $T$, may be generated by many related intentions with the same length; nevertheless, one sequence among all has the highest probability of emergence. In other words, this sequence is the most likely sequence of intentions, which generates the related sequence of activities. The mathematical description of this phase is presented hereafter.

Given a sequence of traces of activities $A_{1:T}$, the estimated parameters $\hat{p}_{\alpha}(a)$ and $\hat{q}(u,v)$ and the initial probabilities for each intention, the VA tries to find the hidden associated intentions’ sequence $I_{1:T}$ which maximizes:

$$P(I_{1:T}|A_{1:T}).$$

(10)

The problem can also be written as:

$$\hat{I}_{1:T} = \arg \max_{I_{1:T}} P(I_{1:T}|A_{1:T})$$

(11)

It is important to highlight that the VA’s output is a sequence of intentions. It enables to account for the history of the users’ activities. In the next section, we detail how we use HMM in a specific case study.

IV. APPLICATION OF HMMs ON REAL DATA

We conducted an experiment in order to obtain traces from students in computer science master’s degree. The process model that was used to guide them was intentionally specified with Map. The dataset obtained from this experiment is discussed in detail in subsection C.

A. Context

In order to get traces, we recorded the activities achieved while creating an Entity-Relationship diagram according to the intentional process model (figure 3) prescribed through a website. The set of students is composed of 71 master students. Table I presents the profile of the students.

<table>
<thead>
<tr>
<th>Total</th>
<th>Average age</th>
<th>Sex</th>
<th>Master degree</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Male</td>
<td>Female</td>
</tr>
<tr>
<td>71</td>
<td>24.4</td>
<td>54</td>
<td>17</td>
</tr>
</tbody>
</table>

The process model presented in Figure 3 is an instance of the Map metamodel [1] that provides a navigational structure that supports the dynamic selection of the next intention to be achieved and the appropriate strategy to achieve it. The Map metamodel allows to specify processes according to actors intentions, and it supports process variability by defining different strategies. Thereby confronted to a specific situation and a particular intention of the user, the process model reveals the alternative strategies to follow the intention, and the intentions to pursue. Hereafter, we give an overview of the intentional process model used in the case study.

B. Intentional process model

The intentional process model represents a process to guide users through the creation of Entity-Relationship diagrams based on [22]. As mentioned earlier, this process is specified with the Map formalism. According to this model, users can select eleven strategies to fulfill three intentions. These intentions are Specify an entity, Specify an association and Stop. Figure 3 shows this intentional process model as a directed graph. Each edge represents a strategy that a user can select to fulfill an intention (specified as a node) according to his/her situation. For instance, if the current situation is Start and the user’s intention is to Specify an entity, there is only one strategy (by completeness of the model) to fulfill this intention. When the current situation is Specify an entity, there are four strategies (by completeness, by generalization, by specialization, by normalization) to fulfill the same intention. It is possible to continue progressing in the process by selecting the strategies that lead to the considered intentions but once the Stop intention is achieved, the enactment of the process is finished. The original map proposed in [22] was more elaborated but we choose to simplify it for this case study.

![Intentional process model](from[22])

To fulfill an intention following a strategy, users have to carry out actions. The term of action differs from activity - the actions are performed by the users but the activities are the user’s actions recorded by an IS tool. There are fifteen actions related to the Map. Table II gives the names of all the actions and Table III shows in detail the link between each section and its related actions.

As can be noted in table III, several actions (consequently several activities) jointly appear simultaneously in intentions Specify an entity and Specify an association, such as delete an attribute. Indeed, a given action can be executed to achieve several different intentions.
TABLE II. SECTIONS AND RELATED TRACE ACTIONS

<table>
<thead>
<tr>
<th>Map Section</th>
<th>Related Trace Actions</th>
<th>Actions Codes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Specify an entity By completeness (model)</td>
<td>Create entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Link attribute to entity</td>
</tr>
<tr>
<td>2</td>
<td>Specify an entity By completeness (entity)</td>
<td>Create attribute</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Link attribute to entity</td>
</tr>
<tr>
<td>3</td>
<td>Specify an entity By normalization</td>
<td>Delete attribute</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Delete Link attribute to entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Delete entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Delete attribute *</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Define primary key</td>
</tr>
<tr>
<td>4</td>
<td>Specify an entity By generalization</td>
<td>Create entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Create specialization link</td>
</tr>
<tr>
<td>5</td>
<td>Specify an entity By specialization</td>
<td>Create entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Create specialization link</td>
</tr>
<tr>
<td>6</td>
<td>Specify an association By reference</td>
<td>Delete attribute</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Create entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Create association</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Link association to entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Link association to entity</td>
</tr>
<tr>
<td>7</td>
<td>Specify an association By expansion</td>
<td>Create association</td>
</tr>
<tr>
<td>10</td>
<td>Specify an association By normalization</td>
<td>Delete association</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(Delete attribute,</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Delete Link attribute to association)</td>
</tr>
<tr>
<td>11</td>
<td>Specify an association By decomposition</td>
<td>Delete attribute</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Create association</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Link association to entity</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Link association to entity</td>
</tr>
<tr>
<td>12</td>
<td>Specify an association By completeness (association)</td>
<td>Create association</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Link attribute to association</td>
</tr>
<tr>
<td>13</td>
<td>Stop By completeness (final)</td>
<td>Create coherency</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Check completeness</td>
</tr>
</tbody>
</table>

* Iterative action

TABLE III. RELATED ACTIONS AND CODES

<table>
<thead>
<tr>
<th>Related Actions</th>
<th>Code</th>
</tr>
</thead>
<tbody>
<tr>
<td>Create entity</td>
<td>A1</td>
</tr>
<tr>
<td>Create association</td>
<td>A2</td>
</tr>
<tr>
<td>Create attribute</td>
<td>A3</td>
</tr>
<tr>
<td>Link attribute to entity</td>
<td>A4</td>
</tr>
<tr>
<td>Link attribute to association</td>
<td>A5</td>
</tr>
<tr>
<td>Link association to entity</td>
<td>A6</td>
</tr>
<tr>
<td>Create generalization link</td>
<td>A7</td>
</tr>
<tr>
<td>Create specialization link</td>
<td>A8</td>
</tr>
<tr>
<td>Define primary key</td>
<td>A9</td>
</tr>
<tr>
<td>Delete attribute</td>
<td>A10</td>
</tr>
<tr>
<td>Delete entity</td>
<td>A11</td>
</tr>
<tr>
<td>Delete association</td>
<td>A12</td>
</tr>
<tr>
<td>Check coherency</td>
<td>A13</td>
</tr>
<tr>
<td>Check completeness</td>
<td>A14</td>
</tr>
<tr>
<td>Delete Link</td>
<td>A15</td>
</tr>
</tbody>
</table>

As a result, it is not trivial to know the intentions of all the actors when executing an action. Our purpose here is to provide a method to find the intentions hidden behind a sequence of activities. The next section applies the HMM previously defined to the dataset described in subsection A, i.e., the traces of users enacting the intentional process model to create Entity-Relationship diagrams.

To be able to record the actors’ traces, we developed a web application with HTML, PHP, JavaScript and MySQL. This application records traces of executions carried out by the users during the creation of their diagrams in a database.

Each record in event log usually contains information about the action that was executed, the process instance it belongs to, and the timestamp of the action execution. The model used to store the traces can be found in [3].

C. Estimation of the parameters of the HMM

Since we monitored the creation of Entity-Relationship diagrams by the users following the intentional process model, it was easy to know the intentions hidden behind the actions traces. The dataset is made of one sequence of actions’ traces and the associated sequence of intentions. In total, we recorded 4141 actions traces produced by 71 students. Consequently, the length of the actions’ traces sequence and the associated intentions is 4141. The knowledge of the intentions enables us to work with the framework of supervised intention mining to estimate the parameters of the HMM. As explained in section III, estimating the parameters of the HMM consists in estimating the coefficients of the matrices $A$ and $I$. Since the intentional process model comprises 3 intentions and 15 actions, the size of $I$ is $3 \times 3$ and the size of $A$ is $3 \times 15$. We obtain the coefficients of the transition matrix $I$ by counting the number of transitions from one intention to another and the coefficients of matrix $A$ by counting the number of times each action trace appears for each intention.
Of course, the quality of the estimated coefficients depends on the length of the sequences used to calculate the estimates. If the length of the sequences is too short, the sequences will not capture all the user behaviors and the estimated coefficients will be of poor quality. On the contrary, if the length of the sequences is long enough, we can capture the typical behaviors of the students and the estimated coefficients will be satisfying. We can verify this phenomenon with our dataset. First, we estimate matrices $A$ and $I$ with the full length of the sequences, i.e., 4141. Then, for eleven different lengths of sequences (1, 5, 10, 20, 30, 40, 50, 100, 200, 300, and 400), we estimate matrices $A$ and $I$ again. We obtain eleven couples of matrices of different quality.

On figure 4, for each sequences’ length, we represent the average difference between the coefficients of estimated matrices $\hat{A}$ and $I$ and the coefficients of the matrices estimated with the full sequences of length 4141. The error of estimation of coefficients decreases with the length of the sequences. For instance, for an estimation over sequences of length 20, the error is 0.15 for the parameters of $\hat{A}$ and 0.08 for the parameters of $I$. Nevertheless, for sequences of length 400, the errors for the transition and emission matrices decrease to 0.05 and 0.001 respectively.

Equations 12 and 13 give, respectively, the estimated matrix of emission of actions in a given intention and the estimated matrix of transition probability for the intentions. We obtain these results for sequences of length 4141. These results are the best estimation of the parameters.

$$\hat{A} = \begin{pmatrix} 0.1276 & 0 & 0.4020 & 0.4020 & 0 & 0 & 0.0008 & 0.0025 & 0.0068 & 0.0240 & 0.0102 & 0 & 0 & 0.0138 \\ 0.0436 & 0.4782 & 0.1239 & 0 & 0.1239 & 0.0873 & 0 & 0 & 0.0768 & 0 & 0.0332 & 0 & 0 & 0.0332 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0.5 & 0.5 & 0 \end{pmatrix}$$

Regarding the intentions, Figure 5 illustrates the process model obtained by the transitions probabilities. We can deduce from these results that when actors enact Specify an entity, they have a high probability (0.9438) to continue performing this intention. They can switch to Specify an association with a probability of 0.0522, and they can go directly to Stop with a probability of 0.004. This last transition is very surprising since it is not allowed in the model given on Figure 3. It means that some of the students deviated from the prescribed process model. When they enact Specify an association, they mostly continue performing this intention with a probability of 0.6771 or switch to Specify an entity with a probability of 0.2775. Once again, this transition is not present in the prescribed process model. Consequently, this is a deviation from the prescribed process model. Finally, when they enact Stop, the only next intention possible is Stop. This is an expected result since two different actions are performed in this intention: check coherency and check completeness. As a result, the action Check coherency is always followed by check completeness. Once a student has performed the two actions of Stop, his/her trace is stopped. Consequently, the following intention comes from another student starting the process with the first intention (Specify an Entity).

Equations 12 and 13 give, respectively, the estimated matrix of emission of actions in a given intention and the estimated matrix of transition probability for the intentions. We obtain these results for sequences of length 4141. These results are the best estimation of the parameters.

$$\hat{I} = \begin{pmatrix} 0.9438 & 0.0522 & 0.0040 \\ 0.2775 & 0.6771 & 0.0454 \\ 0.4588 & 0 & 0.5412 \end{pmatrix}$$

In equation 13, it is important to highlight the coefficient $\hat{I}_{31}$ (0.4588). Indeed, this coefficient would mean that there is a possible transition from Stop to Specify an entity. But we want to make it clear that it is not the case: there is no possible transition from Stop to Specify an entity. The reason why this coefficient is not zero is that we treat the traces of different users sequentially. Consequently, when the trace of a student ends by the intention Stop, it is followed by the trace of another student starting with Specify an entity.

Regarding the emission matrix, we can verify that the actions $\{A_2, A_4, A_5, A_6, A_7, A_9, A_{10}, A_{11}, A_{13}, A_{14}\}$ only appear for a unique intention whereas the other actions $\{A_1, A_3, A_{10}, A_{12}, A_{15}\}$ can appear for several intentions. It is consistent with the definition of the traces of activities given in subsection B and it means that finding the intentions associated...
to these latter actions is a difficult task. With a trivial method, one cannot distinguish which action belongs to which intention.

In terms of actors behaviors, we learned that the most executed actions to Specify an entity are $A_3$ and $A_4$: Create attribute and Link attribute to entity. The most executed action to Specify an association is Create an association. This knowledge is useful to understand the behaviors of the students.

D. Intentions recovery for random actions traces

Once we estimated the parameters of the HMM, we can use them to find the hidden intentions behind any sequence of actions traces, by using the VA. Our interest here is to determine the minimum length of sequences required to estimate the parameters of the HMMs in order to recover the right intentions with the VA. Consequently, we compare the performances of the VA with the eleven couples of estimated matrices obtained with the estimation lengths of 1, 5, 10, 20, 30, 40, 50, 100, 200, 300, and 400.

The comparison protocol is the following: for 1000 test sequences of actions of length 1500, we apply the VA, with each couple of matrices, on each sequence of actions. For each test sequence of actions, we get eleven predicted intentions. By comparing predicted intentions to the actual ones, and averaging the results over the 1000 realizations, we obtain the error percentage associated to each couple of matrices. We present the results in figure 6. It is interesting to note that the number of errors with the VA decreases when the estimated matrices are good. More precisely, with matrices estimated with sequences of length 200, we have an error percentage lower than 5%, which is satisfying.

Recall is the ratio between the number of intentions correctly identified by the VA and the number of intentions in the dataset. Note that it does not take into account the number of intentions falsely identified by the algorithm. Recall is defined by the following expression:

$$ \text{Recall} = \frac{\text{TP}}{\text{TP} + \text{FN}} \quad (14) $$

Precision denotes the ratio between the number of intentions correctly identified by the VA and the number of intentions identified by the algorithm. Precision is defined by:

$$ \text{Precision} = \frac{\text{TP}}{\text{TP} + \text{FP}} \quad (15) $$

In general, it is possible to increase recall to reduce precision and vice versa. F-score is a combination of precision and recall:

$$ \text{Fscore} = \frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}} \quad (16) $$

This is also known as F-1 measure, because precision and recall are weighted equally. F-1 measures the effectiveness of intention’s recovery, considering the same importance for recall and precision.

E. Validation

1) Measures of method validation

In order to evaluate the results that are provided by application of the VA on real data, we choose the recall, precision and F-factor (a combination of recall and precision) measures [29]. Before explaining these measures, we give a brief overview of some terms according to the context of this paper.

We evaluate the accuracy of the VA prediction by checking if the prediction matches to the actual intentions. Table IV shows these definitions:

<table>
<thead>
<tr>
<th>Prediction</th>
<th>True</th>
<th>False</th>
</tr>
</thead>
<tbody>
<tr>
<td>True</td>
<td>True positive (TP)</td>
<td>False positive (FP)</td>
</tr>
<tr>
<td>False</td>
<td>False negative (FN)</td>
<td>True negative (TN)</td>
</tr>
</tbody>
</table>

### Table IV. Prediction and intention

<table>
<thead>
<tr>
<th>Prediction</th>
<th>True</th>
<th>False</th>
</tr>
</thead>
<tbody>
<tr>
<td>True</td>
<td><strong>TP</strong></td>
<td><strong>FP</strong></td>
</tr>
<tr>
<td>False</td>
<td><strong>FN</strong></td>
<td><strong>TN</strong></td>
</tr>
</tbody>
</table>

The True Positives (TP) represents the number of intentions correctly assigned by the VA as belonging to the right class of intention.

The False Negative (FN) represents the number of intentions, which were not assigned to the right class of intention.

The False Positive (FP) represents the number of intentions incorrectly assigned to the class of intention.

We evaluate the accuracy of the VA prediction by checking if the prediction matches to the actual intentions. Table IV shows these definitions:

- Recall
- Precision
- F-score
intentions? The value of the precision ratio is the answer to this question. The precision result stabilizes at 97%, which means 3% of the actions are ill associated to Specify an entity while they belong to other intentions.

The accuracy of retrieval for Specify an association intention, F-1, is measured at 0.87. In other words, when the user intention is Specify an association, the VA is able to find this intention with a very good accuracy.

Regarding the third intention, Stop, all the three measures stabilize at 1, as shown in figure 9, because the actions associated to Stop are not common to other intentions. It is then trivial to identify this intention.

The following table shows the results obtained for the recall, precision and F-score measures for each predefined intentions.

<table>
<thead>
<tr>
<th>Intention</th>
<th>Recall</th>
<th>Precision</th>
<th>F-SCORE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intention 1</td>
<td>99.50%</td>
<td>97%</td>
<td>0.98</td>
</tr>
<tr>
<td>Intention 2</td>
<td>80%</td>
<td>96%</td>
<td>0.87</td>
</tr>
<tr>
<td>Intention 3</td>
<td>100%</td>
<td>100%</td>
<td>1</td>
</tr>
</tbody>
</table>

These results show that we were able to find the intentions behind the activities with satisfying accuracy. The results of F-score prove the efficiency and performance issued of from the application of a HMM applied on our dataset.

V. PERSPECTIVES AND CONCLUSION

This paper shows that HMM is an effective model to retrieve intentions from traces of activities. We used a supervised learning approach and the results shown in our first experimentation are promising. We were able to find the intentions behind the activities with satisfying accuracy, efficiency and performance (table V). Moreover, we also obtain the possibilities of transition from one intention to another (matrix $\hat{I}$) and the probabilities for apparition of activities in each intention (matrix $\hat{A}$), which is a first step to discover the intentional process model.

Another contribution of this work is the definition of a new field of research called Intention Mining, in line with previous works of our team on intentional process models (Nature [32], [33], [34]).
In further works, we will tackle the same problematic of intention discovery using unsupervised learning approach. In this other kind of approach, we do not know the segmentation of activities sequence, i.e., the links between intentions and activities sequences are unknown. We may intent to use the Baum-Welch algorithm [23] procedure, which is a variation of the more general Expectation-Maximization algorithm [12,24].

Another aspect that we plan to study is to find the apparition probability of a given activities’ sequence assuming the parameters of the HMM are known. This perspective is interesting because many different intentions can lead to the same sequence of activities. Consequently, the probabilities for all the possible intentions must be added to get the probability of a given activities sequence.

Since the number of possible intentions increases exponentially with the length of the sequence, the computation of this probability can be quite complex. A solution to overcome this complexity issue is to use Forward-Backward algorithms [10] an inference algorithm for HMMs that compute, for a given observed sequence, the corresponding hidden states.

ACKNOWLEDGMENT

We would like to thank Sébastien Sion for the development of the first version of the web site and the Master Miage students for participating in the experiment.

REFERENCES


[31] S. Das and M.C. Mozer, “A unified gradient Descent/Clustering Architecture for Finite State Machine Induction.” In proceeding of the


